Intelligent fault diagnosis under varying working conditions based on domain adaptive convolutional neural networks

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**ABSTRACT**

Traditional intelligent fault diagnosis typically works well when the labeled training data (source domain) and unlabeled testing data (target domain) are drawn from the same distribution. However, in many real-world applications, this does not hold as the working conditions can vary between training and testing time. In this paper, a Domain Adaptive Convolutional Neural Networks called DACNN is proposed to address the issues of intelligent fault diagnosis when the data at training and test time do not come from the same distribution as a domain adaptation problem. DACNN consists of three parts: a source feature extractor, a target feature extractor, and a label classifier. In order to obtain strong fault-discriminative and domain-invariant capacity, we adopt a two-stage training process. First, to get the fault-discriminative features, the source feature extractor is pre-trained with labeled source training examples to minimize the label classifier error. Then, during the domain adaptive fine-tuning stage, the target feature extractor is trained to minimize the squared Maximum Mean Discrepancy (MMD) between the output of the source and target feature extractor, such that the instances sampled from the source and target domains have similar distributions after the mapping. Moreover, the layers between the source and target feature extractors in our DACNN are partially untied during the training stage in order to take both training efficiency and domain adaptation into consideration.

Experiments on the bearing and gearbox fault data showed that DACNN can achieve high fault diagnosis precision and recall under different working conditions, outperforming other intelligent fault diagnosis methods. We also demonstrate the ability to visualize the learned features and the networks to better understand the reasons behind the remarkable performance of our proposed model.

**INDEX TERMS**

convolutional neural networks, domain adaptation, deep learning, intelligent fault diagnosis, transfer learning

I. INTRODUCTION

\textbf{M}ACHINE health monitoring is of great importance in modern industry. Machine failures could cause great economic loss, and sometimes even pose threats to the people who work with the machines. There is, therefore, an unceasing need to keep the industrial machines working properly and reliably through better and more intelligent machine health monitoring technique [1], [2].

In recent years, deep learning techniques have achieved huge successes in computer vision [3], [4] and speech recognition [5], [6]. Some deep learning techniques have recently found their way into machine health monitoring systems. For example, Jia et al. took the frequency spectra generated by fast Fourier transform (FFT) as the input of a stacked autoencoder (SAE) with three hidden layers for fault diagnosis of rotary machinery components [7]. Zhu et al. proposed a SAE model for hydraulic pump fault diagnosis that used frequency features generated by Fourier transform [8]. Liu
et al. used the normalized spectrum generated by the Short-time Fourier transform (STFT) of sound signals as the input of a SAE model consisting of two layers. Multi-domain statistical features including time domain features, frequency domain features, and time-frequency domain features have also been fed into the SAE model as a way of feature fusion [9], [10]. While there were some researchers focusing on deep belief networks (DBN) [11]–[13], the convolutional neural networks (CNN) [14], [15], which is popular for deep learning for image recognition, is also becoming popular for intelligent fault diagnosis of mechanical parts. For example, 1-D raw time vibration signals were used as the inputs of the CNN model for motor fault detection in [16], which successfully avoided the time-consuming feature extraction process. Guo et al. [17] proposed a hierarchical CNN consisting of two functional layers, where the first part is responsible for fault-type recognition and the other part is responsible for fault-size evaluation.

Most of the above proposed methods work well in the situation when the data used to train classifier and the data for testing are under the same working condition, in other words, under the common assumption that the labeled training data (source domain) and unlabeled testing data (target domain) are drawn from the same distribution. However, this assumption does not hold in practice. As the working condition varies in real-world applications, the labeled data obtained in one working condition may not follow the same distribution in another different working condition. When the distribution changes, most fault diagnosis models need to be rebuilt from scratch using newly recollected labeled training data. However, it is very expensive, if not impossible, to annotate huge amounts of training data in the target domain to rebuild a new model.

As one of the important research directions of transfer learning, domain adaptation (DA) typically aims at minimizing the differences between distributions of different domains in order to minimize the cross-domain prediction error by taking full advantage of information coming from both source and target domains. DA has recently been introduced into the field of fault diagnosis, such as [18]–[22]. For instance, Zhang et al. [20] took 1-D raw time vibration signal as the input of the CNN model, which realize fault diagnosis under different working loads. The domain adaptation capacity of this model originates from the method named Adaptive Batch Normalization (AdaBN). Lu et al. [19] and Wen et al. [22] separately integrated the maximum mean discrepancy (MMD) as the regularization term into the objective function of the deep neural networks (DNN) and the three-layer sparse auto-encoder (SAE) to reduce the differences between distributions cross domains. In general, the main problem for domain adaptation is the divergence of distribution between the source domain and the target domain. We need to learn a feature representation that is both fault-discriminative and simultaneously domain-invariant. The fault-discriminative ability means that the learned feature representation should minimize the label classifier error, i.e., has a good ability to identify different faults. The domain-invariant ability means that instances sampled from the source and target domains should have similar distributions in the learned feature space.

We designed a Domain Adaptive model based on CNN named DACNN, which simultaneously satisfied the above fault-discriminative and domain-invariant requirements. The details of the model will be shown in Section V.

The main contributions of this work are summarized as follows:

- The proposed DACNN consists of three parts, namely, a source feature extractor, a target feature extractor, and a label classifier. We adopt the two-stage training process to train our DACNN to ensure its strong fault-discriminative and domain-invariant capacity. In particular, unlike other existing deep domain adaptation models, we partially untied the layers between the source and target feature extractors in the proposed DACNN to ensure both training efficiency and domain adaptation capability.

The rest of paper is organized as follows. Section II shows the influence of the change in working conditions on the fault diagnosis model. In Section III some preliminary knowledge that will be used in our proposed framework is briefly reviewed. Section IV introduces the construction of our proposed DACNN. A series of experiments on the classic CWRU bearing fault data and the 2009 PHM gearbox fault data are conducted in Section V and Section VI respectively. Finally, we conclude this paper in Section VII.

II. THE INFLUENCE OF THE CHANGE IN WORKING CONDITIONS

Most of the fault diagnosis models work well only under a common assumption: The training and test data are drawn from the same distribution. However, in real-world applications of fault diagnosis, the working conditions (e.g., motor load and speed) may change from time to time according to the requirements of the production. The distributions of data collected from different working conditions are similar but nonetheless different. For example, the training samples for building the classifier may be collected from the work condition without motor load, while the resulting classifier is used to classify the defects of a bearing system under different motor load states. The target data distributions with various motor load states will be different from the source data distribution for training the fault diagnostic classifier, even though the categories of defects to be detected have remained unchanged.

In order to show the influence of the change in working conditions on the fault diagnosis model, the motor bearing signals provided by Case Western Reserve University (CWRU) [23] and the state-of-the-art two-stage intelligent fault diagnosis method proposed by Lei [24] are analyzed in this section.

The vibration signals were collected from the drive end of a motor in the test rig under four different conditions: 1) normal condition; 2) inner-race faults (IF); 3) outer-race faults (OF); and 4) ball fault (BF). For IF, OF, and BF...
cases, vibration signals for three different severity levels (0.007 inches, 0.014 inches, and 0.021 inches) were separately collected. The sampling frequency was 12 kHz and the signals were all collected under four working conditions with different motor load and rotating speed, i.e., Load0 = 0hp/1797rpm, Load1 = 1hp/1772rpm, Load2 = 2hp/1750rpm and Load3 = 3hp/1730rpm. Further details regarding the data description can be found in section 1.

According to the description given by Lei [24], there are 100 samples for each health condition under one load, where each sample is a vibration signal of bearings containing 1200 data points. Therefore, the motor bearing dataset totally contains 4000 samples, namely \( D_{\text{ALL}} \), which consists of four working conditions.

In the first learning stage, local discriminative features are extracted from raw vibration signals from \( D_{\text{ALL}} \) by whitening, sparse filtering and local feature averaging. PCA is implemented on the learned features, and their first three PCs are shown in Figure 1(a). As illustrated in Figure 1(a), without considering the working conditions of the samples, most samples of the same health condition are gathered in the corresponding cluster and most samples of the different health conditions are separated. However, in order to show the influence of the change in working conditions on the distributions of the data, we mark the samples collected from working condition Load3 and Load1 separately in Figure 1(b). From Figure 1(b), we can find that the change in working conditions obviously affected the distributions of the samples of partial health conditions, such as 0.007/IF (Inner-race Faults with severity level of 0.007 inches), 0.007/BF, 0.007/OF, 0.014/BF and 0.021/IF.

![Figure 1](image1.png)

**FIGURE 1:** Scatter plots of PCs for the learned features. Ten different kinds of faults are denoted by ten different colors respectively. (a) the motor bearing dataset \( D_{\text{ALL}} \) consists of four working conditions. (b) the motor bearing dataset consists of two working conditions, where cross symbols represent the working condition Load3 and square symbols represent the working condition Load1.

In the second stage, the soft-max regression model is applied by Lei [24] to classify mechanical health conditions using the learned features. We implement the soft-max regression model using the Tensorflow toolbox of Google and keep all the parameter settings the same as Lei [24] did. Similarly, in order to demonstrate the effect of the change in working conditions on the fault diagnosis accuracy, two models are trained separately. The first soft-max regression model is trained by 10% of samples randomly selected from \( D_{\text{ALL}} \), and the testing accuracy is 99.6% with a small standard deviation. The accuracy’s and loss’s trends are visualized in Figure 2. Then, 10% of samples collected from the working condition Load3 are randomly selected to train the second soft-max regression model and tested by all of the samples collected from the working condition Load1. Figure 3 shows the corresponding accuracy’s and loss’s trends. The validating accuracy is 99%, but the testing accuracy is merely 78.02%.

![Figure 2](image2.png)

**FIGURE 2:** The first soft-max regression model trained by 10% of samples randomly selected from \( D_{\text{ALL}} \). (a) The training accuracy’s and test accuracy’s trends. (b) The training loss’s and test loss’s trends.

![Figure 3](image3.png)

**FIGURE 3:** The second soft-max regression model trained by randomly selecting 10% of samples collected from the working condition Load3 and tested by all of the samples collected from the working condition Load1. (a) The training accuracy’s, validating accuracy’s and test accuracy’s trends. (b) The training loss’s, validating loss’s and test loss’s trends.

From the above-mentioned experimental results, we can conclude that the change in working conditions does change...
the distribution of the data and affect the accuracy of the fault diagnosis model severely. Therefore, the goal of this paper is to be able to predict labels given a sample from one working condition correctly while the classifier is trained by the samples collected from another working condition.

III. PRELIMINARY KNOWLEDGE

A. DOMAIN ADAPTATION

The above practical problem of varying working conditions for fault diagnosis can be regarded as a domain adaptation (DA) problem. According to the survey on domain adaptation for classification [25], a domain $D$ consists of two components: a feature space $X$ and a marginal probability distribution $P_X$, where $X \in \mathcal{X}$. Given a specific domain, a task $T$ consists of two components: a label space $\mathcal{Y}$ and a prediction function $f(X)$. Given a source domain $D_S$ and a corresponding learning task $T_S$, a target domain $D_T$ and a corresponding learning task $T_T$, domain adaptation aims to improve the learning of the target predictive function $f_T$ in $D_T$ using the knowledge in $D_S$ and $T_S$, where $D_S \neq D_T$ and $T_S = T_T$, i.e., the tasks are the same but the domains are different.

The problem of fault diagnosis under varying working conditions can be framed as a domain adaptation problem by regarding samples collected from different working conditions as different domains:

- The feature spaces between domains are the same, $\mathcal{X}^S = \mathcal{X}^T$ (e.g., the fast Fourier transform (FFT) spectrum amplitudes of raw vibration temporal signals), but the marginal probability distributions of the input data are different, $P_X^S \neq P_X^T$.
- The label spaces between domains are the same, $\mathcal{Y}^S = \mathcal{Y}^T = \{1, \ldots, K\}$, where $K$ is the number of fault types.

B. DOMAIN DIVERGENCE MEASURE

The main problem in domain adaptation is the divergence of distribution between the target domain and source domain. Ben-David et al. [26], [27] defines a divergence measure $d_{H\Delta H}(P_X^S, P_X^T)$ between two domains $D_S$ and $D_T$, which is widely used in the theory of nonconservative domain adaptation. Using this notion, they established a probabilistic bound on the performance $\epsilon_T(h)$ of some label classifier $h$ evaluated on the target domain $D_T$ given its performance $\epsilon_S(h)$ on the source domain $D_S$. Formally,

$$\epsilon_T(h) \leq \epsilon_S(h) + \frac{1}{2} d_{H\Delta H}(P_X^S, P_X^T) + \lambda, \quad (1)$$

where $\lambda$ is supposed to be a negligible term and does not depend on classifier $h$.

Eq. [1] tells us that to adapt well, one has to learn a label classifier $h$ which works well on source domain while reducing the $d_{H\Delta H}(P_X^S, P_X^T)$ divergence between $D_S$ and $D_T$.

C. MAXIMUM MEAN DISCREPANCY

Many criteria can be used to estimate the divergence of distribution between different domains, such as Kullback-Leibler (K-L) divergence and Maximum Mean Discrepancy (MMD) [28]. Different from K-L divergence, which needs an intermediate density estimation, MMD is a nonparametric estimation criterion for comparing distributions of data sets based on Reproducing Kernel Hilbert Space (RKHS).

Given observations $X_S = \{x^i_S\}_{i=1}^{N_S}$ and $X_T = \{x^i_T\}_{i=1}^{N_T}$, drawn independently and identically distributed (i.i.d.) from $P_X^S$ and $P_X^T$ respectively, the empirical estimate of the squared MMD in a reproducing kernel Hilbert space $\mathcal{H}$ with associated continuous kernel $k(\cdot, \cdot)$ can be formulated as follows:

$$MMD^2(X_S, X_T) = \frac{1}{N_S^2} \sum_{i,j=1}^{N_S} k(x^i_S, x^j_S) - \frac{2}{N_S N_T} \sum_{i=1}^{N_S} \sum_{j=1}^{N_T} k(x^i_S, x^j_T) + \frac{1}{N_T^2} \sum_{i,j=1}^{N_T} k(x^i_T, x^j_T). \quad (2)$$

$MMD(X_S, X_T)$ vanishes if and only in $P_X^S = P_X^T$, when $N_S, N_T \to \infty$.

IV. PROPOSED DOMAIN ADAPTIVE CNN

A. PROBLEM FORMALIZATION

Let the labeled source domain data be $D_S = \{(x^i_S, y^i_S)\}_{i=1}^{N_S}$, where $x^i_S \in \mathbb{R}^{m \times 1}$ is the data instance, $y^i_S \in \{1, \ldots, K\}$ is its corresponding class label, and $D_T = \{(x^i_T)\}_{i=1}^{N_T}$ is the unlabeled target domain data. Here, $N_S$ and $N_T$ are the numbers of instances in $D_S$ and $D_T$.

The overall framework of the proposed Domain Adaptive CNN (DACNN) is shown in Figure 4. It includes a source feature extractor $M_S$, a target feature extractor $M_T$, and a source classifier $C_T$, which together form a deep feed-forward architecture that maps each input sample $x^i_S$ (resp. $x^i_T$) to a $K$-dimensional feature vector $M_S(x^i_S)$ (resp. $M_T(x^i_T)$) ($K$ equals to the number of class label) and predicts its class label $y \in \{1, \ldots, K\}$.

We use the following two-stage training procedure to enhance the domain adaptation ability of our model:

1) **Pre-training** the source feature extractor $M_S$ to minimize the label prediction loss $\epsilon_S(C)$ for the labeled source domain samples.

2) Initialize the parameters of the target feature extractor $M_T$ with the pre-trained source feature extractor $M_S$, then perform **domain adaptive fine-tuning** to obtain fault-discriminative and simultaneously domain-invariant feature extractors by partially untying higher layers between $M_S$ and $M_T$.

During testing, unlabeled target examples are mapped with the target feature extractor $M_T$ to the latent feature space and classified by the source label classifier $C$. 

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Our work is primarily motivated by the probabilistic bound in Eq. 1 proposed by Ben-David et al. in 2010. Based on this bound, to adapt well, one has to learn a label classifier which works well on source domain while reducing the divergence of distribution between domains. This inspired the current proposed two-stage training procedure. Firstly, the pre-training stage corresponds to learning a label classifier \( C \) which works well on the source domain using the labeled source domain samples. Then, the domain adaptive fine-tuning stage corresponds to making a trade-off between reducing the divergence between domains and maintaining classifier’s performance on the labeled source domain data. The divergence is measured by the squared MMD between domains in our proposal.

Moreover, similar to our model, the Deep Adaptation Networks (DAN) [29] applies the multiple kernel variant of MMD (MK-MMD) for the purpose of minimizing the difference between the source and target feature distributions under the higher layers of CNN. Different from our two-stage training procedure, the DAN chooses to simultaneously fine-tune the CNN on the source labeled examples and update the higher fully connected layers for the source and target examples respectively by adding an MK-MMD-based multi-layer adaptation regularizer to the CNN risk. However, we choose to separately train the feature extractor \( M_S \) and \( M_T \) in the two-stage procedure. Because the target domain has no labeled samples, and the feature extractor \( M_T \) may quickly learn a degenerate solution if we don’t initialize those higher untied layers in \( M_T \) by the parameters of the pre-trained source feature extractor \( M_S \). Actually, the DAN also faces the problem of how to initialize the parameters of the higher fully connected layers for the unlabeled target domain. Unlike our model, they choose to start with an AlexNet model pre-trained on ImageNet 2012.

We are now ready to present each step of the proposed framework.

**B. PRE-TRAINING**

As shown in Figure 5, we compose the source feature extractor \( M_S \) from multiple convolutional layers and fully-connected layers. The input of the first convolution layer can be the fast Fourier transform (FFT) spectrum amplitudes of vibration signals, which is the most widely used approach of fault detection. The last fully-connected layer is called label layer [30] with an output of \( K \) neurons (equals to the number of the class label), which is fed to label classifier \( C \) to estimate the posterior probability of each class. It is common to add a pooling layer after each convolution layer in the CNN architecture separately. It functions as a down-sampling operation which results in a reduced-resolution output feature map, which is robust to small variations in the location of features in the previous layer. The most commonly used pooling layer is the max-pooling layer, which performs the local max operation over the input features. In order to capture the useful information in the intermediate and low-frequency bands, the wide kernels should be used in the first convolutional layer which can better suppress high-frequency noise [20]. The following convolutional kernels become gradually smaller which make the networks deeper to acquire good representations of the input signals and improve the performance of the networks.

For an source domain instance \( x^S_i \), the output feature
vector \( M_S(x^i_S) \in \mathbb{R}^{K \times 1} \) mapped by the source feature extractor \( M_S \) is the input of the label classifier \( C \). Here, the soft-max regression model \([31]\) is used as the label classifier on the source domain to incorporate label information. The soft-max regression model is a generalization of the logistic regression model for multi-class classification problems. We can estimate the probabilities of each class that \( x^i_S \) belongs to as follows,

\[
C(M_S(x^i_S)) = \begin{bmatrix} p(y = 1|x^i_S) \\ p(y = 2|x^i_S) \\ \vdots \\ p(y = K|x^i_S) \end{bmatrix} = \frac{1}{\sum_{j=1}^{K} e^{u_j}} \begin{bmatrix} e^{u_1} \\ e^{u_2} \\ \vdots \\ e^{u_K} \end{bmatrix},
\]

where \( u_j = M_S(x^i_S)^T j \) is the \( j \)-th value of \( M_S(x^i_S) \), \( \sum_{j=1}^{K} e^{u_j} \) is a normalized term, and \( p(y = j|x^i_S) \) represent the distribution of the class \( j \in \{1, 2, \ldots, K\} \) given the instance \( x^i_S \).

The details of the pre-training step are shown in Algorithm 1. Given the source domain data \( D_S \), the parameters of the source feature extractor \( M_S \) can be derived by minimizing the following cost function,

\[
L_{cls}(D_S) = \frac{1}{N_S} \sum_{i=1}^{N_S} \sum_{j=1}^{K} 1\{y^i_S = j\} \log C(M_S(x^i_S))_j,
\]

where \( 1\{y^i_S = j\} \) is an indicator function, whose value is 1 if \( y^i_S = j \), otherwise 0.

### C. DOMAIN ADAPTIVE FINE-TUNING

Given that the target domain is unlabeled, we first initialize the parameters of the target feature extractor \( M_T \) with the pre-trained source feature extractor \( M_S \).

As shown in Figure 6, we choose to learn the parameters of the target feature extractor \( M_T \) by partially untying higher layers between the source and target mappings, which is based on the following two reasons.

Firstly, the approaches of most published domain adaptation models can be summarized into two categories: symmetric transformation and asymmetric transformation. For many prior symmetric transformation methods \([32], [33]\), all layers are constrained, thus enforcing exact source and target mapping consistency. Although learning a symmetric transformation can reduce the number of parameters in the model, this may make the optimization poorly conditioned, since the same networks must handle samples from two separate domains \([34]\). The intuitive idea behind the asymmetric transformation is to constrain a subset of the layers. Rozantsev et al. \([35]\) showed that partially shared weights can lead to effective adaptation in both supervised and unsupervised settings.

Second, in the standard CNN, deep features must eventually transition from general to specific by the last layer of the networks, and the transferability gap grows with the domain discrepancy and becomes particularly large when transferring the higher layers.

For an instance \( x^i_S \) (resp. \( x^i_T \)), the output feature vector \( M_S(x^i_S) \) (resp. \( M_T(x^i_T) \)) mapped by the feature extractor \( M_S \) (resp. \( M_T \)) is denoted by \( \xi^i_S \) (resp. \( \xi^i_T \)). Since there are no labeled data in the target domain, we propose to learn the divergence between domains by the squared MMD distance.
between their marginal distributions $P_{M_S(x_S)}$ and $P_{M_T(x_T)}$. So, a good trade-off between reducing the divergence between domains and maintaining classifier’s performance on the labeled source domain data can be achieved by adding the following squared MMD based domain adaptation regularizer \( \frac{\lambda}{2} \) to the cost function of label classifier \( C \) \( \frac{\lambda}{2} \).

$$
\min_{M_S,M_T} L_{cls} + \lambda MMD^2(\xi_S, \xi_T),
$$

where \( \lambda > 0 \) is a trade-off parameter. We then assume that such \( M_S \) and \( M_T \) satisfy \( P_{Y|M_S(x_S)} \approx P_{Y|M_T(x_T)} \). The details are shown in Algorithm 2.

On the other hand, the output of the last fully-connected layer could be regarded as a type of conditional distribution over the classes, and the output of other layers could be taken as the marginal distribution of features. Although the MMD matching is only done on the last layer of the networks in our current model, all the parameters of the untied layers of the target feature extractor \( M_T \) are updated during the process of back-propagation in the domain adaptive fine-tuning stage. Therefore, in the process of parameter updating, the domain discrepancy underlying both the marginal distribution and the conditional distribution could be essentially reduced.

**D. TESTING**

After all the parameters are learned, we can construct a classifier for the target domain by directly using the output of the last fully-connected layer of the target feature extractor \( M_T \). As shown in Figure 7, for any instance \( x_T \) in the target domain, the output of the target feature extractor \( M_T(x_T) \) can compute the probability of instance \( x_T \) belonging to the label \( j \in \{1, ..., K\} \) using Eq. 5. We choose the maximum probability using Eq. 6 and the corresponding label \( j \) as the prediction.

$$
y_T^* = \max_j \frac{e^{u_j}}{\sum_{m=1}^K e^{u_m}}, \text{ with } u_j = M_T(x_T^j).
$$

**V. CASE STUDY 1: FAULT DIAGNOSIS OF ROLLING BEARING USING THE PROPOSED METHOD**

Rolling bearings are the most commonly used components in rotating machinery, and bearing faults may result in significant breakdowns, and even casualties [37], [38]. However, learning an effective fault diagnostic model is challenging as the training vibration signals used for bearing fault diagnosis might be collected under the work condition without the motor load, while the actual application is to classify the defects from a bearing system under different motor load states. As the target data distribution changes with varying motor loads, the machine learning model must be able to use unlabeled
Domain adaptive fine-tuning

**Function** \text{Finetune}():

**Data:**
- Given one source domain \( D_S = \{(x_i^S, y_i^S)\}_{i=1}^{N_S} \) and one target domain \( D_T = \{(x_i^T)\}_{i=1}^{N_T} \).
- The parameters of the pre-trained source feature extractor \( M_S \).
- The number of adaptive layers, \( l \).
- The number of trade-off parameter, \( \lambda \).

**Result:** The parameters in the target feature extractor \( M_T \).

**begin**
- Initialize the parameters of the target feature extractor \( M_T \) with the pre-trained source feature extractor \( M_S \).

**for number of training iterations do**
- Sample minibatch of \( m \) instances \( \{(x_i^S, y_i^S), \ldots, (x_i^m, y_i^m)\} \) from the source domain \( D_S \).
- Sample minibatch of \( m \) instances \( \{x_1^T, \ldots, x_m^T\} \) from the target domain \( D_T \).
- Update the final \( l \) adaptive layers of the source feature extractor \( M_S \) by ascending its stochastic gradient:
  \[ \nabla_{M_S} (L_{cls} + \lambda MMD^2(\xi_S, \xi_T)) \]
- Update the final \( l \) adaptive layers of the target feature extractor \( M_T \) by ascending its stochastic gradient:
  \[ \nabla_{M_T} \lambda MMD^2(\xi_S, \xi_T) \]

**end**

**end**

FIGURE 7: Third training step - Testing.

Data under any load condition to rebuild the classifier trained with samples collected in one load condition. In this section, we demonstrate the effectiveness of the proposed DACNN method for fault detection under this scenario on the bearing fault dataset provided by Case Western Reserve University (CWRU) Bearing Data Center.

### A. DATASETS AND PREPROCESSING

The basic layout of the test rig is shown in Figure 8. It consists of a 2 hp motor (left), a torque transducer/encoder (center), a dynamometer (right), and control electronics (not shown). The test bearings support the motor shaft. Further details regarding the test rig can be found at the CWRU Bearing Data Center website [23].

Drive end bearing faulty data are adopted in this study. Subjected to electro-sparking, inner-race faults (IF), outer-race faults (OF) and ball fault (BF) with different sizes (0.007 inches, 0.014 inches, and 0.021 inches) are introduced into the drive-end bearing of the motor. Outer-race faults are stationary faults, therefore placement of the fault relative to the load zone of the bearing has a direct impact on the vibration response of the motor/bearing system. In order to quantify this effect, the outer-race faults themselves are grouped into three categories according to the fault position relative to the load zone: 'centered' (fault in the 6 o’clock position), 'orthogonal' (3 o’clock) and 'opposite' (12 o’clock). The vibration signals were sampled by the accelerometers attached to the rack with magnetic bases under the sampling frequency of 12 kHz and were post-processed in a Matlab environment. The experimental scheme simulates three working conditions with different motor load and rotating speed, i.e., Load1 = 1hp/1772rpm, Load2 = 2hp/1750rpm and Load3 = 3hp/1730rpm. The vibration signals of normal bearings (NO) under each working condition are also gathered. All data files released by the CWRU Bearing Data Center are in Matlab (*.mat) format. Each data file corresponds to one kind of data under one working condition and is defined by a unique file ID. For example, the file '106.mat' contains the data of the fault type '0.007/IF' collected from Load1 (i.e., Domain A). The details of the chosen data and its corresponding file ID are described in Table 1.
In this paper, a vibration signal with length 4096 is randomly selected from the raw vibration signal. Then, the fast Fourier transform (FFT) is implemented on each signal and the 4096 Fourier coefficients are generated. Since the coefficients are symmetric, the first 2048 coefficients are used in each sample. The samples collected from the above three different conditions form three domains, namely A, B, and C, respectively. There are ten classes under each working condition, including nine kinds of faults and a normal state, and each class consists of 800 samples. Therefore, each domain contains 8000 samples of ten classes collected from the corresponding working condition.

To construct domain adaptation problems, we randomly choose two from the three domains, where one is considered as the source domain and the other is considered as the target domain. Therefore, we construct six ($P_3^2$) domain adaptation problems. Take the domain adaptation problem $A \rightarrow B$ as an example. The examples of domain A are used as the source domain data $D_S$, and the examples of domain B are used as the target domain data $D_T$.

**B. EXPERIMENTAL SETUP**

1) Baseline Methods

We compare our methods with the following state-of-the-art fault diagnosis methods:

1) The deep neural networks (DNN) system with frequency features [7] proposed by Lei et al. in 2016. This neural networks consists of three hidden layers. The number of neurons in each layer is 1025, 500, 200, 100 and 10. The input of the networks is the normalized 1025 Fourier coefficients transformed from the raw temporal signals using FFT.

2) The two-stage intelligent fault diagnosis method proposed by Lei et al. in 2016. [24]. In the first learning stage, local discriminative features are extracted from raw vibration signals by whitening, sparse filtering and local feature averaging. In the second stage, the softmax regression model is applied to classify mechanical health conditions using the learned features.


2) Parameters of the proposed DACNN

The feature extractors $M_S$ and $M_T$ used in our experiments are composed of five convolutional layers and pooling layers followed by two fully-connected hidden layers. The pooling type is max pooling and the activation function is ReLU.

The principles of selecting the hyperparameters of the feature extractors $M_S$ and $M_T$ are introduced in Section [V-B] i.e., the wide kernels should be used in the first convolutional layer which can better suppress high-frequency noise and the following convolutional kernels become gradually smaller which make the networks deeper to acquire good representations of the input signals and improve the performance of the
networks. Based on these principles and extensive parameter tuning, we determine the parameters of the convolutional and pooling layers detailed in Table 2. In order to minimize the loss function, the Adam Stochastic optimization algorithm is applied to train our CNN model. The final $l$ ($l \in [1, 7]$) layers of the target feature extractor $M_T$ are untied and used as adaptive layers.

The experiments are implemented using the Tensorflow toolbox of Google and a sum of $m$ multiple Gaussian kernels $\{k_i(x, x') = \exp(-\frac{(x-x')^2}{2\sigma_i^2})\}$ is applied as the kernel function $k(x, x')$ to parameterize the target feature extractor $M_T$, i.e., $k(x, x') = \sum_{i=1}^{m} k_i(x, x')$. Exponentially growing sequence of the parameter $\sigma_i$ is used for each Gaussian kernel $k_i$ (for example, $\sigma_i = 10^{-5}, 10^{-2}, 10^{-1}, 10, 10^1, 10^2, 10^3$).

During the pre-training stage, we randomly select 75% of the source labeled instances to train the $M_S$ and remaining is for validation. Then, during the domain adaptive fine-tuning stage, we use $A$-distance as a measure of domain discrepancy which is suggested by Ben-David et al. [27], and automatically select the parameter of $l$ and $\lambda$ by assessing the $A$-distance. It involves the following steps:

1) Pseudo-labeling the output feature vectors $\xi_S$ and $\xi_T$ with 0 and 1.
2) Randomly sampling two sets of instances from $(\xi^i_S, 0)_{i=1}^{N_S}$ and $(\xi^i_T, 1)_{i=1}^{N_T}$ as the training and testing set.
3) Learning a two-sample classifier (SVM in our case) as domain classifier to distinguish the input instances between the source and target domains on the training set and verifying its performance on the testing set.
4) Estimating the $A$-distance as $d_A = 2(1 - \epsilon)$, where $\epsilon$ is the test error.

It's obvious that if two domains perfectly overlap with each other, $\epsilon \approx 0.5$, and $d_A \approx 0$. On the contrary, if two domains are completely distinct from each other, $\epsilon \approx 0$, and $d_A \approx 2$. Therefore, $d_A \in [0, 2]$. The lower the value is the smaller two domains divergence.

To compare the effectiveness of domain adaptation, for an instance from the target domain $x^i_T$, we use the corresponding output of the pre-trained source feature extractor $M_S(x^i_T)$ to compute the probability of the instance $x^i_T$ belonging to a label $j \in \{1, ..., K\}$ using Eq. [3] which is denoted as DACNN$^S$.

**C. ACCURACY ACROSS DIFFERENT DOMAINS**

As Table 3 shows, DNN performed poorly in domain adaptation, with average accuracies in the six scenarios being around 78.05%, which prove that samples under different working conditions draw from the different distributions and existing models trained under one working condition is not suitable for fault classification under another working condition.

https://github.com/tensorflow/models/blob/master/research/domainadaptation/domain_separation/utils.py

Compared with the two-stage fault diagnosis method using sparse filter and WDCNN with AdaBN with average accuracy being 96.37% and 95.95% respectively, DACNN achieves the best accuracy in the average of 99.60%. This result proves that the features learned by DACNN are more domain invariant than the features learned by the other methods.

In addition, by comparing DACNN with DACNN$^S$, we can find that in every scenario, the performance of DACNN is superior to DACNN$^S$. This means that the domain adaptation fine-tuning stage can significantly improve the fault diagnosis under varying working conditions.

It is also interesting that when adapting from Domain A to B, from B to A, from B to C, and from C to B, the fault diagnosis accuracy of the proposed DACNN is a bit better than WDCNN (AdaBN). However, when adapting from domain A to C and C to A, the proposed DACNN is significantly better than the other methods.

**D. SENSITIVITY ANALYSIS OF FAULTS**

Accuracy has been widely used as the metric to evaluate the fault diagnosis model. However, fault diagnosis is by definition an imbalanced classification problem where the positive class (machine faults) is greatly outnumbered by the negative class. The accuracy metric is therefore not an appropriate measure for assessing model performance - a classifier with a focus on merely getting all the negative instances correct will have a high accuracy by definition, but it will not be useful for identifying the few positive instances (i.e. machine faults) when it really matters. We need a metric that assesses the model’s ability to find all the relevant cases in the dataset so that a good model does not miss the relevant cases. Also, in the case of fault diagnosis, the cost of false positives (e.g. halting the production line for unnecessary maintenance) can be quite high. As such, we need another useful metric that tells us out of those predicted positive, precisely how many of them are actually positive. As such, in this work we propose to employ two additional evaluation indicators, i.e. precision and recall, which have been widely used in other fields such as pattern recognition, information retrieval, and binary classification, to assess the two aspects of the model performance respectively.

In the fault diagnosis context, the precision and recall for a fault type $f$ can be calculated as below,

$$\text{precision}(f) = \frac{\text{TP}}{\text{TP} + \text{FP}}, \quad \text{recall}(f) = \frac{\text{TP}}{\text{TP} + \text{FN}},$$

where true positives (TP) means the number of faults correctly identified as $f$, false positives (FP) means the number of faults incorrectly labeled as $f$ and false negatives (FN) means the number of faults $f$ incorrectly labeled as not belonging to $f$.

A precision score of 1.0 for a fault type $f$ means that every sample labeled as belonging to class $f$ does indeed belong to class $f$ (i.e. there is no false alarm), but it can’t tell us about
the number of samples from class $f$ that were not labeled correctly (i.e. how many failures are missing?).

Whereas a recall of 1.0 means that every item from a fault type $f$ was labeled as belonging to class $f$ (i.e. there is no missing alarm), but says nothing about how many other items were incorrectly also labeled as belonging to class $f$ (i.e. how many false alarms are there?).

The precision and recall of every class processed by DACNN and DACNN$_S$ are detailed in Table 4 and Table 5.

In Table 4 for the 3rd kinds of fault (i.e. IF with fault size being 0.014 in.), DACNN$_S$ has low precision when adapting from domain B to C and from C to A, which are 49.63% and 57.55% respectively. This means that about half of that kind of fault alarms are unreliable.

Meanwhile, in Table 5 for the 2nd kinds of fault (i.e. IF with fault size being 0.007 in.), DACNN$_S$ has very low recall when adapting from domain B to C and from C to A, which are 1.13% and 26.75% respectively. This means that about a large number of that kind of failures are not detected.

In general, the precision and recall of DACNN are higher than that of DACNN$_S$, which implies that DACNN has fewer false alarms (i.e. high precision score) and missed alarms (i.e. high recall score). Smith et al have pointed out that the ball fault cases are the most difficult to diagnose [29]. This is consistent with our experimental results. We can find that DACNN can make almost all class classified into right class, except BF with fault size being 0.014 in and BF with fault size being 0.021 in. This result shows that after the domain adaptive fine-tuning stage, the classification performance on every class achieves remarkable improvement.

### E. PARAMETER SENSITIVITY

In this section, we investigate the influence of the parameter $l$, which represents the number of untied layers in the target feature extractor $M_T$ during the domain adaptive fine-tuning stage.

Given that the target feature extractor $M_T$ contains five convolutional layers and pooling layers and two fully-connected hidden layers, $l$ is selected from $\{1, ..., 7\}$ in our experiment. We use DACNN$_l$ to denote the DACNN model with the parameter $l$. For example, DACNN$_1$ indicates that only the last fully-connected hidden layer is untied (i.e. FC2 in Figure 4), and DACNN$_7$ means all the seven layers in $M_T$ are untied (i.e. from ‘Conv1’ to ‘FC2’ in Figure 4). Figure 9 reports the results.
reduce the distribution discrepancy across domains. We can generally observe that the more untied layers involved in the domain adaptive fine-tuning stage, the higher the accuracy of recognition.

However, the sensitivity of different adaptive problems to parameters $i$ is different. When adapting from domain A to B, the enhancement of recognition accuracy is limited. We can use DACNN$_S$ directly to achieve the accuracy of 99.86%, which is only a little worse than DACNN$_7$. For the domain adaptation from A to C, and from C to B, we only need to untie the last three fully-connected hidden layers (i.e. DACNN$_3$) to achieve the same highest accuracy as DACNN$_7$.

Moreover, the distribution differences between domains are not symmetrical. By contrast, we have to respectively untie the last six layers (i.e. DACNN$_6$) for the domain adaptation from B to A and from C to A and untie the last five layers (i.e. DACNN$_5$) for the domain adaptation from B to C to achieve the best accuracy as DACNN$_7$.

### F. NETWORKS VISUALIZATIONS

Deep learning is often viewed as an empirical success rather than a mathematical solution to the learning problem. In order to understand better why the proposed DACNN model can achieve the remarkable performance in bearing fault diagnosis under varying working conditions, the features extracted by the $M_S$ and $M_T$ are visualized in this subsection.

**t-Distributed Stochastic Neighbor Embedding (t-SNE)** is a technique for dimensionality reduction that is widely used for the visualization of the deep neural networks. The goal of t-SNE is to take a set of points in a high-dimensional space and find a faithful representation of those points in a lower-dimensional space, typically the 2D plane. In this paper, t-SNE is used to visualize the features extracted by DACNN. For more details about t-SNE, we refer to Ref. [40].

Take the domain adaptation task $B \rightarrow C$ as an example, t-SNE is used to visualize the high-dimensional features extracted by the source feature extractor $M_S$ and the target feature extractor $M_T$. The result is shown in Figure 10. In all subgraphs of Figure 10, features of the source sample $\{x_S^i\}_{i=1}^{N_S}$ are extracted by $M_S$, i.e., $M_S(x_S^i)_{i=1}^{N_S}$, which is represented by square symbols. For the target sample, features extracted by $M_S$ (i.e., $M_S(x_T^i)_{i=1}^{N_T}$) are shown in (a) and features extracted by the fine-tuning $M_T$ after 1000 and 2000 iterations are shown in (b) and (c). For convenience, these features are denoted by $M_S(x_S)$, $M_S(x_T)$ and

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**TABLE 4: precision of the proposed DACNN$_S$ and DACNN on six domain adaptation problems.**

<table>
<thead>
<tr>
<th>Fault location</th>
<th>None</th>
<th>IF</th>
<th>BF</th>
<th>OF (Centered @6:00)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Diameter (in.)</td>
<td>0.007</td>
<td>0.014</td>
<td>0.021</td>
<td>0.007 0.014 0.021</td>
</tr>
<tr>
<td>Category labels</td>
<td>1 2 3 4 5 6 7 8 9 10</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

**TABLE 5: recall of the proposed DACNN$_S$ and DACNN on six domain adaptation problems.**

<table>
<thead>
<tr>
<th>Fault location</th>
<th>None</th>
<th>IF</th>
<th>BF</th>
<th>OF (Centered @6:00)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Diameter (in.)</td>
<td>0.007</td>
<td>0.014</td>
<td>0.021</td>
<td>0.007 0.014 0.021</td>
</tr>
<tr>
<td>Category labels</td>
<td>1 2 3 4 5 6 7 8 9 10</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
where the number of iterations \( it \) is selected from \{1000, 2000\}.

There are some interesting observations as follows.

1) \( M_S(x_S), M_T(x_T) \) and \( M_T^{it}(x_T) \) are classifiable when they are diagnosed separately. This illustrates that the CNN used for \( M_S \) and \( M_T \) has a very strong ability to distinguish various rolling bearing faults and explains the reason why DACNN\(_S\) can even achieve such a good classification accuracy.

2) In Figure 10(a), the distribution of fault ‘0.007/IF’ is completely different between domains. This explains why DACNN\(_S\) has the very low recall of 1.13\% when adapting from domain B to C.

3) During the domain adaptive fine-tuning stage, with the increasing of iterations, the distributions of features between \( M_S(x_S) \) and \( M_T^{it}(x_T) \) gradually become consistent. When the features \( M_T^{1000}(x_T) \) and \( M_T^{2000}(x_T) \) are applied to fault detection, the accuracies are 99.75\% and 99.90\% respectively.

Finally, we visualize all nodes in the entire DACNN model, including \( M_S \), \( M_T \) and the soft-max outputs of the label predictor \( C \). We randomly select a sample of the fault type ‘0.007/IF’ from domain C, denoted by \( x_C^{0.007/IF} \), as the input of the DACNN model trained for adapting from domain B to domain C. The visualized results are shown in Figure 11(a) and Figure 11(b).

From these visual results, we can find out that the output of the first three convolutional layers (i.e. ‘Conv1’, ‘Conv2’ and ‘Conv3’) are very similar. Starting from the fourth layer convolution layer (i.e. ‘Conv4’), the extracted features of \( M_S(x_C^{0.007/IF}) \) and \( M_T(x_C^{0.007/IF}) \) gradually change to some extent. This observation is consistent with the result in the section V-E. That is, for the domain adaptation from B to C, we only have to untie last four layers starting from ‘Conv4’ to ‘FC2’ as the features extracted from the first three convolutional layers are almost the same.

The last fully-connected layer (i.e. ‘FC2’) has \( K \) neurons (equals the number of the class label). The output of ‘FC2’ is fed to label classifier \( C \) to estimate the posterior probability of each class using soft-max regression model.

According to the results of ‘FC2’ and ‘Softmax’ in Figure 11(a), \( x_C^{0.007/IF} \) is misdiagnosed as the fault type of ‘0.014/IF’, based on the extracted features of \( M_S(x_C^{0.007/IF}) \). As a contrast, in Figure 11(b), \( x_C^{0.007/IF} \) is correctly identified as the fault type of ‘0.007/IF’, based on the extracted features of \( M_T(x_C^{0.007/IF}) \).

![Visualization of all nodes in \( M_S \), \( M_T \) and the soft-max results of the label predictor \( C \).](image)

**FIGURE 11:** Visualization of all nodes in \( M_S \), \( M_T \) and the soft-max results of the label predictor \( C \). Domain B is the source domain and domain C is the target domain.

**VI. CASE STUDY 2: FAULT DIAGNOSIS OF GEARBOX USING THE PROPOSED METHOD**

In this section, the 2009 PHM data challenge of gearboxes [41] is used to evaluate the effectiveness of the proposed method.

**A. DATASETS AND PREPROCESSING**

The 2009 PHM gearbox fault data are representative of generic industrial gearbox data, which contains 3 shafts, 4 gears, and 6 bearings. Two geometries are used, one using a spur gears, the other using helical gears. Data were sampled synchronously from accelerometers mounted on both the input and output shaft retaining plates. Another attached tachometer generates 10 pulses per revolution providing very accurate zero crossing information. The schematic of the gearbox used to collect the data is shown in Figure 12.

The experimental dataset is comprised of six different health conditions. The detailed description of the health conditions is shown in Table 6. For each health condition, signals were collected at 30, 35, 40, 45 and 50 Hz shaft speed under high and low load, with a sampling frequency of 66.67 kHz and acquisition time of 4 s. In this section, only the input channel of the vibration signals of the helical gearbox under low load is used to test the performance of the proposed method.

![Diagram of gearbox](image)
FIGURE 10: Visualization of the extracted features of samples collected from the source domain B and target domain C via t-SNE. Ten different kinds of faults are denoted by ten different colors respectively. Features of the source domain B extracted by $M_S$ are represented by square symbols in all subgraphs. Features of the target domain C extracted by $M_S$ (i.e., $M_S(x_T)$) are shown in (a) and features extracted by the fine-tuning $M_T$ after 1000 and 2000 iterations are shown in (b) and (c).

Table 6: Health conditions of the 2009 PHM data challenge of gearboxes.

<table>
<thead>
<tr>
<th>Category labels</th>
<th>Gear</th>
<th>Bearing</th>
<th>Shaft</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>24 T</td>
<td>Others</td>
<td>Input Shaft : Output Side</td>
</tr>
<tr>
<td>1</td>
<td>Good</td>
<td>Good</td>
<td>Good</td>
</tr>
<tr>
<td>2</td>
<td>Chipped</td>
<td>Good</td>
<td>Good</td>
</tr>
<tr>
<td>3</td>
<td>Broken</td>
<td>Good</td>
<td>Combination</td>
</tr>
<tr>
<td>4</td>
<td>Good</td>
<td>Good</td>
<td>Combination</td>
</tr>
<tr>
<td>5</td>
<td>Broken</td>
<td>Good</td>
<td>Good</td>
</tr>
<tr>
<td>6</td>
<td>Good</td>
<td>Good</td>
<td>Good</td>
</tr>
</tbody>
</table>

Vibration signals are divided into data segments at first and 6144 sampling points are selected as a segment [42]. Then, the fast Fourier transform (FFT) is implemented on each data segment and the first 4097 coefficients are used in each sample. The samples collected from 30, 35, 40, 45 and 50 Hz shaft speed form five domains. There are six classes under each working condition and each class consists of 800 samples. Therefore, each domain contains 4800 samples of six classes collected from the corresponding working condition.

We randomly choose two from the five domains to construct domain adaptation problems, where one is considered as the source domain and the other is considered as the target domain. Therefore, we construct twenty ($P_d^2$) domain adaptation problems. Take the domain adaptation problem $30Hz \rightarrow 40Hz$ as an example. The examples collected at 30 Hz shaft speed are used as the source domain data $D_S$, and the examples collected at 40 Hz shaft speed are used as the target domain data $D_T$.

B. EXPERIMENTAL SETUP

1) Baseline Methods

We compare our methods with the convolutional neural networks (CNN) system with frequency features [42] proposed...
by Jing et al. in 2017. This CNN consists of one convolutional layer, one pooling layer and a fully-connected layer with softmax. Table 7 lists the parameters of the CNN. Neither overlapping of the convolutional window nor padding is used in their experiments. The input of the networks is the 4097 Fourier coefficients transformed from the data segments with length 6144 of the raw temporal signals using FFT.

According to the experimental setting in [42], the CNN is trained by 50% of samples randomly selected from the dataset composed of 6 different health conditions of the gearbox under low load and 30, 40, 50 Hz speed. PCA is implemented on the FFT features, and their first three PCs are shown in Figure 13. As illustrated in Figure 13 without considering the working conditions of the samples, most samples of the same health condition are gathered in the corresponding cluster and most samples of the different health conditions are separated. The testing accuracy is 99.33% with a small standard deviation. The accuracy’s and loss’s trends of CNN [42] are visualized in Figure 14.

However, we can find that the mean and variance of the data collected at different speeds have changed significantly. Then, 50% of samples collected from the 30 Hz speed are randomly selected to train the other CNN model and tested by all of the samples collected from the 40 Hz speed. Figure 15 shows the corresponding accuracy’s and loss’s trends of CNN [42]. The validating accuracy is nearly 100%, but the testing accuracy is merely 27%.

![Figure 13](image1.png)

**FIGURE 13:** Scatter plots of PCs for the FFT features. Six different kinds of health conditions are denoted by six different colors respectively, where cross symbols represent the 30 Hz speed, square symbols represent the 40 Hz speed and dot symbols represent the 50 Hz speed.

![Figure 14](image2.png)

**FIGURE 14:** The CNN model trained by 50% of samples randomly selected from the dataset composed of 6 different health conditions of the gearbox under 30, 40, 50 Hz speed. (a) The training accuracy’s and test accuracy’s trends. (b) The training loss’s and test loss’s trends.

![Figure 15](image3.png)

**FIGURE 15:** The CNN model trained by randomly selecting 50% of samples collected from the 30 Hz speed and tested by all of the samples collected from the working condition the 40 Hz speed. (a) The training accuracy’s, validating accuracy’s and test accuracy’s trends. (b) The training loss’s, validating loss’s and test loss’s trends.

2) Parameters of the proposed DACNN

Similar to Case Study 1, the feature extractors \( M_S \) and \( M_T \) are composed of five convolutional layers and pooling layers followed by two fully-connected hidden layers. The pooling type is max pooling and the activation function is ReLU. The parameters of the convolutional and pooling layers are detailed in Table 8. Also, we apply a sum of \( m \) multiple Gaussian kernels \( \{ k_i(x, x') = \exp\left(-\frac{\|x-x'\|^2}{2\sigma_i^2}\right) \} \) as the kernel function \( k(x, x') \) and exponentially growing sequences of the parameter \( \sigma_i \) is used to estimate the largest MMD distance between domains during the domain adaptive fine-tuning.

By comparing Figure 13 and Figure 14, we can find that the changes in the mean and variance of the gearbox dataset are more obvious than the bearing dataset. In order to make the examples of the gearbox dataset more or less look like standard normally distributed data and accelerate the convergence of the training of the feature extractors \( M_S \) and
TABLE 7: Parameters of the CNN used by [42].

<table>
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<th>stride</th>
<th>Channel</th>
<th>Output</th>
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<td>2033 x 8</td>
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<td>1</td>
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<td>1 4</td>
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</table>

Table 8: Details of the feature extractor $M_S$ and $M_T$ used in experiments.

<table>
<thead>
<tr>
<th>No.</th>
<th>Layer type</th>
<th>Layer name</th>
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<th>stride</th>
<th>Channel</th>
<th>Output</th>
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</tbody>
</table>

C. ACCURACY ACROSS DIFFERENT DOMAINS

Each subgraph of Figure 16 represents the accuracy of four domain adaptive problems when the examples collected at the corresponding shaft speed are used as the source domain data. The solid line in each subgraph represents the difference of the shaft speed $\Delta_{speed}$ between the domains. We can find that the accuracy of fault diagnosis generally decreases with the increase of $\Delta_{speed}$.

As Table 9 shows, CNN [42] performed poorly in domain adaptation, with average accuracy in the twenty domain problems being around 33.21%. Also, when the $\Delta_{speed}$ is 5 Hz, its average accuracy in the corresponding eight domain problems is merely 50.66%. By contrast, DACNN achieves 82.62% accuracy in average in the twenty domain problems. And, its average accuracy is 91.22% in the eight domain problems with the $\Delta_{speed}$ being 5 Hz.

TABLE 9: Average Accuracy (%) on $\Delta_{speed}$. The numbers in parentheses represent the amount of corresponding domain adaptive problems.

<table>
<thead>
<tr>
<th>$\Delta_{speed}$</th>
<th>5 Hz (8)</th>
<th>10 Hz (6)</th>
<th>15 Hz (4)</th>
<th>20 Hz (2)</th>
<th>AVG</th>
</tr>
</thead>
<tbody>
<tr>
<td>CNN</td>
<td>50.66%</td>
<td>26.03%</td>
<td>17.33%</td>
<td>16.67%</td>
<td>33.21%</td>
</tr>
<tr>
<td>DACNN</td>
<td>76.06%</td>
<td>66.29%</td>
<td>56.61%</td>
<td>38.46%</td>
<td>65.48%</td>
</tr>
<tr>
<td>DACNN</td>
<td>91.22%</td>
<td>81.55%</td>
<td>74.29%</td>
<td>68.02%</td>
<td>82.62%</td>
</tr>
</tbody>
</table>

In addition, by comparing CNN with DACNN$_S$, we can find that in every scenario, the performance of DACNN$_S$ is superior to CNN. The use of z-score in the training phase which makes the examples of the gearbox dataset look like standard normally distributed data plays an important role.

FIGURE 17: The DACNN$_S$ model trained by 50% of samples randomly selected from the dataset composed of 6 different health conditions of the gearbox under low load and 30, 40, 50 Hz speed. (a) The training accuracy’s and test accuracy’s trends. (b) The training loss’s and test loss’s trends.

FIGURE 18: The DACNN$_S$ model trained by randomly selecting 50% of samples collected from the 30 Hz speed and tested by all of the samples collected from the working condition the 40 Hz speed. (a) The training accuracy’s, validating accuracy’s and test accuracy’s trends. (b) The training loss’s, validating loss’s and test loss’s trends.
Similar to the experimental setting in [42], the DACNN$_S$ is trained by 50% of samples randomly selected from the dataset composed of 6 different health conditions of the gearbox under low load and 30, 40, 50 Hz speed. The accuracy’s and loss’s trends of the DACNN$_S$ are visualized in Figure 17.

Then, 50% of samples collected from the 30 Hz speed are randomly selected to train the other CNN model and tested by all of the samples collected from the 40 Hz speed. Figure 18 shows the corresponding accuracy’s and loss’s trends of the DACNN$_S$. From Figure 17 and Figure 18, we can find that the training of the DACNN$_S$ can converge faster than CNN and its accuracy’s and loss’s trends are more stable.

**VII. CONCLUSION**

This paper proposes a domain adaptive model based on CNN named DACNN to address the fault diagnosis problem under varying working condition. DACNN contains three parts, a source feature extractor, a target feature extractor, and a label classifier. Unlike other existing domain adaptation models, the layers between the source and target feature extractor in the proposed DACNN are partially untied during the training stage to ensure both training efficiency and effective domain adaptation. In order to obtain strong fault-discriminative and domain-invariant capacity, we adopt a two-stage training process. First, to get the fault-discriminative features, the source
feature extractor is pre-trained with labeled source training examples to minimize the label classifier error. Then, during the domain adaptive fine-tuning stage, the target feature extractor is initialized and trained to minimize the squared MMD between the output of the source and target feature extractor, such that the instances sampled from the source and target domains have similar distributions after the mapping.

Results on the classic CRWU bearing fault data in Section VI and the 2009 PHM gearbox fault data in Section VI demonstrate that, compared with the state-of-the-art intelligent fault diagnosis models, the proposed DACNN achieves higher accuracy under different working conditions. Besides the commonly used fault diagnostic accuracy, we also employed in this work two additional evaluation metrics, namely precision and recall, to analyze the sensitivity of the proposed for each type of fault detection. A precision score of 1.0 for a fault type means that there is no false alarm, while a recall of 1.0 means that there is no missing alarm. Compared with accuracy, precision and recall can evaluate the reliability of a model for certain type of fault recognition in more details.

Finally, through visualizing the feature maps learned by our model, we explored the inner mechanism of our proposed model in fault diagnosis and domain adaptation and verified that partially untying of the layers between the source and target feature extractor can lead to effective adaptation.

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REFERENCES


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