## COURSE OUTLINE: MH5201

| Course Title | Advanced Investigations in Linear Algebra II |  |
| :--- | :--- | :--- |
| Course Code | MH5201 |  |
| Offered | Study Year X, Semester 2 |  |
| Course Coordinator | Xia Kelin (Asst Prof) | XIAKELIN@ntu.edu.sg |
| Pre-requisites | MH1201 OR Approval by Division of Mathematical Sciences |  |
| Co-requisites | MH1201 |  |
| AU | 1 |  |
| Contact hours | Tutorials: 26 |  |
| Approved for delivery from | AY 2022/23 semester 2 |  |
| Last revised | 10 Jan 2023, 11:44 |  |

## Course Aims

The course will introduce the advanced materials in linear algebra, in particular, determinants, eigenvalues and eigenvectors, and the deep relations between matrixes, vector spaces, determinants and eigenvalue and eigenvectors. The course will focus on the advanced and challenging problems in these topics and the application of these topics in sciences.

## Intended Learning Outcomes

Upon successfully completing this course, you should be able to:

1. Solve complex problems in determinants
2. Solve complex problems in eigenvalues and eigenvectors
3. Solve complex problems in linear algebra that require a better understanding of deep relations between matrices, vector spaces, determinants and eigenvalue and eigenvectors
4. Apply advanced linear algebra knowledge in sciences
5. Solve abstract versions of problems in determinants, eigenvalues, eigenvectors, matrices and advanced linear algebra

## Course Content

Different kinds of challenging problems for determinant and how to approach them.
Various challenging problems for eigenvalues and eigenvectors and their solutions
Challenging problems that requires a better understanding of the deep relations between matrixes, vector spaces, determinants and eigenvalue and eigenvectors.

Applications of matrix, vector space, determinant, and eigenvalue and eigenvector in sciences.

Assessment

| Component | Course ILOs tested | SPMS-MAS <br> Graduate Attributes tested | Weighting | Team / Individual | Assessment Rubrics |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Continuous Assessment |  |  |  |  |  |
| Tutorials |  |  |  |  |  |
| Quiz 1 | 1,2,3, 5 | 1. $\mathrm{a}, \mathrm{b}, \mathrm{c}$ | 20 | individual | See Appendix for rubric |
| Quiz 2 | 1,2,3, 5 | 1. a, b, c | 20 | individual | See Appendix for rubric |
| Project | 4, 5 | 1. a <br> 2. a <br> 3. $a, b$ <br> 4. a | 20 | individual | See Appendix for rubric |
| Mid-semester Quiz |  |  |  |  |  |
| Midterm Examination | 1, 2, 3, 5 | 1. a, b, c | 40 | individual | See Appendix for rubric |
|  |  | Total | 100\% |  |  |

These are the relevant SPMS-MAS Graduate Attributes.

## 1. Competence

a. Independently process and interpret mathematical theories and methodologies, and apply them to solve problems
b. Formulate mathematical statements precisely using rigorous mathematical language
c. Discover patterns by abstraction from examples
2. Creativity
a. Critically assess the applicability of mathematical tools in the workplace
3. Communication
a. Present mathematics ideas logically and coherently at the appropriate level for the intended audience
b. Work in teams on complicated projects that require applications of mathematics, and communicate the results verbally and in written form
4. Civic-mindedness
a. Develop and communicate mathematical ideas and concepts relevant in everyday life for the benefits of society

## Formative Feedback

Test and quizzes: Feedback on common mistakes and the level of difficulty of the problems is given. Students will receive individual feedback on their performance in the class, quiz and test during the classes.

Group Project: Feedbacks on performance in the group project will also be given to each group of students.

## Learning and Teaching Approach

| Tutorials <br> $(26$ <br> hours $)$ | This will help to develop problem solving skills, and reinforce the understanding of the concepts <br> and notions. |
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## Reading and References

Gilbert Strang, Linear Algebra and Its Applications, 2006, Cengage Learning, ISBN: 9780030105678

Roger A. Horn, Charles R. Johnson, Matrix Analysis Second Edition, 2012, Cambridge, ISBN: 9780521548236

## Course Policies and Student Responsibilities

Absence Due to Medical or Other Reasons

If you are sick and not able to attend a quiz or midterm, you have to submit the original Medical Certificate (or another relevant document) to the administration to obtain official leave. In this case, the missed assessment component will not be counted towards the final grade. There are no make-up quiz or make-up midterm.

Academic Integrity \& Collaboration Policy
Good academic work depends on honesty and ethical behaviour. The quality of your work as a student relies on adhering to the principles of academic integrity and to the NTU Honour Code, a set of values shared by the whole university community. Truth, Trust and Justice are at the core of NTU's shared values.

As a student, it is important that you recognize your responsibilities in understanding and applying the principles of academic integrity in all the work you do at NTU. Not knowing what is involved in maintaining academic integrity does not excuse academic dishonesty. You need to actively equip yourself with strategies to avoid all forms of academic dishonesty, including plagiarism, academic fraud, collusion and cheating. If you are uncertain of the definitions of any of these terms, you should go to the academic integrity website for more information. Consult your instructor(s) if you need any clarification about the requirements of academic integrity in the course.
Collaboration is encouraged for your homework because peer-to-peer learning helps you understand the subject better and working in a team trains you to better communicate with others. As part of academic integrity, crediting others for their contribution to your work promotes ethical practice.
You must write up your solutions by yourself and understand anything that you hand in. If you do collaborate, you must write on your solution sheet the names of the students you worked with. If you did not collaborate with anyone, please explicitly write, "No collaborators." Failure to do so constitutes plagiarism

Use of materials outside the course is strongly discouraged. If you use outside source, you must reference it in your solution.

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## Course Instructors

Instructor Office Location Phone Email

Planned Weekly Schedule
Week

| Topic | Course <br> ILO | Readings/ Activities |  |
| :--- | :--- | :--- | :--- |
| 1 | Challenging problems for determinant | 1 | Solve problems |
| 2 | Challenging problems for determinant | 1 | Solve problems |
| 3 | Challenging problems for determinant | 1 | Solve problems |
| 4 | Challenging problems for eigenvalues and eigenvectors | 2 | Solve problems |
| 5 | Challenging problems for eigenvalues and eigenvectors | 2 | Solve problems |
| 6 | Challenging problems for eigenvalues and eigenvectors | 2 | Solve problems |
| 7 | Challenging and advanced problems for linear algebra | 3 | Solve problems |
| 8 | Challenging and advanced problems for linear algebra | 3 | Solve problems |
| 9 | Challenging and advanced problems for linear algebra | 3 | Solve problems |
| 10 | Challenging and advanced problems for linear algebra | 3 | Solve problems |
| 11 | The application of matrix, vector space, determinant, and <br> eigenvalue and eigenvector in sciences. | 4 | Presentation (Group <br> projects) |
| 12 | The application of matrix, vector space, determinant, and <br> eigenvalue and eigenvector in sciences. | 4 | Presentation (Group <br> projects) |
| 13 | The application of matrix, vector space, determinant, and <br> eigenvalue and eigenvector in sciences. | 4 | Presentation (Group <br> projects) |

## Appendix 1: Assessment Rubrics

Rubric for Tutorials: Quiz 1 (20\%)
Point-based marking (not rubrics based)
Rubric for Tutorials: Quiz 2 (20\%)
Point-based marking (not rubrics based)

Rubric for Tutorials: Project (20\%)

| Grading Criteria | Exceptional (18-20) | Effective (15-18) | Acceptable (12-15) | Developing (0-12) |
| :--- | :--- | :--- | :--- | :--- |
| Accuracy | The interpretation is <br> highly accurate, <br> concise and precise. | The interpretation is <br> mostly accurate. <br> Some parts can be <br> better explained or <br> more succinct. | The interpretation is <br> somewhat accurate. <br> However, it contains <br> some inaccuracies, <br> missing points or <br> ideas that are not <br> related to the <br> interpretation. | The interpretation <br> are mostly <br> inaccurate. |
| Thoroughness | The literature review <br> was comprehensive <br> and rigorous. It <br> includes several <br> different perspectives, <br> including a good <br> spread of the first and <br> latest ideas on the <br> topic. | The literature review <br> was mostly <br> comprehensive and <br> rigorous. It can <br> improve in terms of <br> the selection of the <br> works relating to the <br> topic. | The literature review <br> was adequate. It <br> covers some of the <br> major works relating <br> to the topic. <br> References to <br> primary source is <br> largely missing. | The literature <br> review was not <br> thorough. It is <br> based on a single <br> source of <br> information and/or <br> inaccurate or <br> unreliable <br> secondary sources. |
| Presentation | Very clear and <br> organized. It is easy to <br> follow your train of <br> thought | Mostly clear and <br> organized. Some <br> parts can have better <br> transitions. | Somewhat clear. It <br> requires some <br> careful reading to <br> understand what you <br> are writing. | Mostly unclear and <br> messy. It is difficult <br> to understand what <br> you are writing as <br> there is no clear <br> flow of ideas. |
| Question and <br> Answer (for <br> each individual <br> student) | Very clear and precise <br> answers to all <br> problems. Explain the <br> problems from various <br> different perspectives <br> logically. | Correct answers to <br> most of the problems. <br> Explain the problems <br> in an organized way. | Partially-correct <br> answers to most of <br> the problems. <br> Explain the some of <br> the problems. | Unclear and messy <br> answers. Difficult to <br> understand. |

Rubric for Mid-semester Quiz: Midterm Examination (40\%)
Point-based marking (not rubrics based)

